

for Harry

TITLE 'COLLEEN FLOATING POINT ROUTINES BY C SHAW'

MORE ACCURATE VERSIONS OF THE FOLLOWING SHEPARDSON ROUTINES

EXP, EXP10, LOG, LOG10, SIN, COS, ATAN, SQR AND POWER

THESE ROUTINES WERE TAKEN FROM THE CALCULATOR CARTRIDGE AND MODIFIED
 MANY OTHER MATH FUNCTIONS SUCH AS TAN, ARCSIN AND ARCCOS ARE ALSO
 INCLUDED IN THAT CARTRIDGE.

0095	CR	=	\$9B	; ATASCII CARRIAGE RETURN
0005	GETREC	=	5	; GET RECORD
0009	PUTREC	=	9	; PUT RECORD
0342	ICCOM	=	\$342	
0344	ICBAL	=	\$344	
0348	ICMIL	=	\$348	
E456	CIOV	=	\$E456	

FLOATING POINT SUBROUTINES

0006	FPREC	=	6	; FLOATING PT PRECISION (# OF BYTES)
				IF CARRY USED THEN CARRY CLEAR => NO ERROR, CARRY SET => ERROR
D800	AFP	=	\$D800	; ASCII->FLOATING POINT (FP)
				INBUFF+CIX -> FRO, CIX, CARRY
D8E6	FASC	=	\$D8E6	; FP -> ASCII FRO-> LBUFF (INBUFF)
D9AA	IEP	=	\$D9AA	; INTEGER -> FP
				0-\$FFFF (LSB,MSB) IN FRO, FRO+1->FRO
D9D2	FPI	=	\$D9D2	; FP -> INTEGER FRO -> FRO, FRO+1, CARRY
DA60	FSUB	=	\$DA60	; FRO <- FRO - FR1, CARRY
DA66	FADD	=	\$DA66	; FRO <- FRO + FR1, CARRY
DADB	FMUL	=	\$DADB	; FRO <- FRO * FR1, CARRY
DB28	FDIV	=	\$DB28	; FRO <- FRO / FR1, CARRY
DD89	FLDOR	=	\$DD89	; FLOATING LOAD REGO FRO <- (X,Y)
DD98	FLDIR	=	\$DD98	; " " REG1 FR1 <- (X,Y)
DDA7	FSTOR	=	\$DDA7	; FLOATING STORE REGO (X,Y) <- FRO
DDB6	FMOVE	=	\$DDB6	; FR1 <- FRO
DD40	PLYEVL	=	\$DD40	; FRO <- P(Z) = SUM(I=N TO 0) (A(I)*Z**I) CARRY
				INPUT: (X,Y) = A(N), A(N-1) ... A(0) -> PLYARG
				ACC = # OF COEFFICIENTS = DEGREE+1
				FRO = Z
DDC0	EXP	=	\$DDC0	; FRO <- E**FRO = EXP10(FRO * LOG10(E)) CARRY
DCC	EXP10	=	\$DDCC	; FRO <- 10**FRO CARRY
DECD	LOG	=	\$DECD	; FRO <- LN(FRO) = LOG10(FRO)/LOG10(E) CARRY
DED1	LOG10	=	\$DED1	; FRO <- LOG10 (FRO) CARRY

THE FOLLOWING ARE IN BASIC CARTRIDGE

SIN	=	\$BD81	; FRO <- SIN(FRO) DEGFLG=0 => RADS, 6=> DEG CARRY
COS	=	\$BD73	; FRO <- COS(FRO) CARRY
ATAN	=	\$BE43	; FRO <- ATAN(FRO) CARRY
SQR	=	\$BEB1	; FRO <- SQUAREROOT(FRO) CARRY

FLOATING POINT ROUTINES ZERO PAGE (NEEDED ONLY IF F.P. ROUTINES ARE CALLED)

00D4	FRO	***+FPREC	; FP REGO
00DA	FRE	***+FPREC	
00E0	FR1	***+FPREC	; FP REG1
00E6	FR2	***+FPREC	

FLOATING POINT ROUTINES ZERO PAGE (NEEDED ONLY IF F.P. ROUTINES ARE CALLED)

0004	FRD	***+PREC	, FP REG0
000A	FRE	***+FPREC	
00D0	FRI	***+FPREC	, FP REG1
00F0	FRI	***+FPREC	

COLLEEN FLOATING POINT ROUTINES BY C SHAW

00EC	FRX	***+1	, FP SPARE
00ED	EXEP	***+1	, VALUE OF E
00EE	NSIGN	***+1	, SIGN OF #
00EF	ESIGN	***+1	, SIGN OF EXPONENT
00F0	FCARFLG	***+1	, 1ST CHAR FLAG
00F1	DIORT	***+1	, # OF DIGITS RIGHT OF DECIMAL
00F2	IX	***+1	, CURRENT INPUT INDEX
00F3	INBUFF	***+2	, POINTS TO USER'S LINE INPUT BUFFER
00F5	ZTEMP1	***+2	
00F7	ZTEMP4	***+2	
00F9	ZTEMP5	***+2	
00FB	RADFLG	***+1	, 0=RADIANS, 6=DEGREES
00FD	FLPTR	***+2	, POINTS TO USER'S FLOATING PT NUMBER
00FE	FFIR2	***+2	

FLOATING PT ROUTINES' NON-ZERO PAGE RAM (NEEDED ONLY IF F.P. ROUTINES CALLED)

057E	LBPR1	***+1	, LBUFF PREFIX 1
057F	LBPR2	***+1	, LBUFF PREFIX 2
0580	LBUFF	***+128	, LINE BUFFER
05E0	PLYARG	=	LBUFF+\$60 , POLYNOMIAL ARGUMENTS
05E6	FPSCR	=	PLYARG+FPREC
05EC	FPSCR1	=	FPSCR+FPREC
05E6	FSCR	=	FPSCR
05EC	FSCR1	=	FPSCR1

COLLEEN FLOATING POINT ROUTINES BY C SHAW

FP PACKAGE EQUATES FOR SIN, COS, ATAN, AND SQR ROUTINES ETC

0008	NATCF	=	\$B	; NUMBER OF ATAN COEFFICIENTS FOR POLYNOMIAL EVALUATION
0006	NSCF	=	6	; NUMBER OF SIN COEFFICIENTS
D905	FASC2	=	\$D905	; AFTER FASC (FINISH FP TO ASCII CONVERSION)
D920	XEFORM	=	\$D920	; !EFORM PROCESS E FORMAT FOR FP -> ASCII CONVERSION
D928	XEFORM2	=	\$D928	; AFTER XEFORM (FINISH CONVERSION)
DA44	ZFRO	=	\$DA44	; FRO <- 0
DA46	ZF1	=	\$DA46	; CLEAR 6 BYTES STARTING AT 0.X
DA51	INTLBF	=	\$DA51	; INIT LBUFF INTO INBUFF FOR FP -> ASCII CONVERSION
DC00	NORM	=	\$DC00	; NORMALIZE FLOATING POINT NUMBER - USED BY STRUNC ONLY
DC70	XCVFRO	=	\$DC70	; !CVFRO FP TO 10 ASCII DIGITS IN LBUFF
DE03	EXP1	=	\$DE03	; MIDDLE OF EXP10 WHERE PLYEVL IS CALLED
DE12	EXP11	=	\$DE12	; AFTER PLYEVL IN EXP10
DE89	LOG10E	=	\$DE89	; LOGTEN(E) = .4342944819
DE95	XFORM	=	\$DE95	; FRO <- (FRO-(X,Y)) / (FRO+(X,Y))
DF6C	PHALF	=	\$DF6C	; FLOATING POINT CONSTANT .5
DFAE	ATCDEF	=	\$DFAE	; ATAN COEFFICIENTS
DFFA	FP95	=	\$DFFA	; FLOATING POINT CONSTANT .9999999999 (ALMOST 1)
DFF0	PIOV4	=	\$DFF0	; FLOATING POINT CONSTANT PI/4 = .7853981634

VARIABLES

		== \$480	
0480	QUADFLG	==*+1	; SIN QUADRANT FLAG
0481	INTFLG	==*+1	; FLAG FOR POWER ROUTINE
0482	FIEMP	==*+6	; TEMPORARY FLOATING POINT REGISTER FOR POWER ROUTINE

COLLEEN FLOATING POINT ROUTINES BY C SHAW

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                                **=$A000                ; ARBITRARY STARTING POINT

                                TEST PROGRAM

A000                                START
A000 20 4C A0                      JSR     GETNUM
A003 20 B6 DD                      JSR     FMOVE
A006 20 4C A0                      JSR     GETNUM                ; GET 2ND NUMBER FROM E: -- OMIT IF ONLY ONE ARGUMENT

A009 20 CE A0                      JSR     SP0WER                ; CHANGE TO GET DIFFERENT ROUTINES

A00C 90 0A                          BCC     NOERR

                                ERROR -- DISPLAY MESSAGE

A00E A9 79                          LDA     #ERRMSG
A010 BD 44 03                      STA     ICBAL
A013 A9 A0                          LDA     #ERRMSG/256
A015 4C 32 A0                      JMP     CONTIN

A018                                NOERR
A018 20 E6 DB                      JSR     FASC                ; FLOATING POINT TO ASCII

                                FIND END OF STRING AND CHANGE NEGATIVE # TO POSITIVE AND ADD CARRIAGE RETURN.

A01B A0 FF                          LDY     #$FF
A01D                                MLOOP
A01D C8                            INY
A01E B1 F3                          LDA     (INBUFF),Y
A020 10 FB                          BPL     MLOOP
A022 29 7F                          AND     #$7F
A024 91 F3                          STA     (INBUFF),Y
A026 C8                            INY
A027 A9 9B                          LDA     #CR
A029 91 F3                          STA     (INBUFF),Y

                                DISPLAY RESULT

A02B A5 F3                          LDA     INBUFF
A02D BD 44 03                      STA     ICBAL
A030 A5 F4                          LDA     INBUFF+1
A032                                CONTIN
A032 BD 45 03                      STA     ICBAL+1
A035 A9 09                          LDA     #PUTREC
A037 BD 42 03                      STA     ICCDM
A03A A9 28                          LDA     #40
A03C BD 48 03                      STA     ICBLL
A03F A9 00                          LDA     #0
A041 BD 49 03                      STA     ICBLL+1
A044 A2 00                          LDX     #0
A046 20 56 E4                      JSR     CIOV

A049 4C 00 A0                      JMP     START                ; DO IT AGAIN

A04C                                GETNUM
A04C A9 05                          LDA     #GETREC                ; GET ONE NUMBER FROM E: (ICB #0)
A04E BD 42 03                      STA     ICCDM                ; GET RECORD (ENDS IN CR)

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A04C		GETNUM		,GET ONE NUMBER FROM E (ICCB #0)
A04C A9 05	LDA	#GETREC		,GET RECORD (ENDS IN CR)
A04E BD 42 03	STA	ICCOM		

COLLEEN FLOATING POINT ROUTINES BY C SHAW

A051 A9 80	LDA	#LBUFF		
A053 BD 44 03	STA	ICBAL		
A056 A9 05	LDA	#LBUFF/256		
A058 BD 45 03	STA	ICBAL+1		
A05B A9 28	LDA	#40		
A05D BD 48 03	STA	ICBLL		
A060 A9 00	LDA	#0		
A062 BD 49 03	STA	ICBLL+1		
A065 A2 00	LDX	#0		
A067 20 56 E4	JSR	CIOV		
A06A A9 80	LDA	#LBUFF		
A06C 85 F3	STA	INBUFF		
A06E A9 05	LDA	#LBUFF/256		
A070 85 F4	STA	INBUFF+1		
A072 A9 00	LDA	#0		
A074 85 F2	STA	CIX		
A076 4C 00 DB	JMP	AFP		, CALL ASCII TO FLOATING POINT AND RETURN

A079 45 52 52	ERRMSG	BYTE	"ERROR",CR	
A07C 4F 52 9B				, INDICATES CARRY SET RETURN FROM FP ROUTINE

FRO ← E^FRO

USES INTEGER FUNCTION LIKE BASIC'S INSTEAD OF JUST IFP, WHICH ROUNDS
PROVIDES ACCURACY OF AT LEAST 7 DIGITS (EXCEPT POSSIBLY AT EXTREMA)
INSTEAD OF 6.

```

A07F          SEXPE          ;E^X (SEE SHEP ATARI BASIC $DDCO EXP)
A07F A2 B9    LDX          #LOG10E      ;E^X = 10^(X*LOGTEN(E))
A081 A0 DE    LDY          #LOG10E/256
A083 20 E8 A2 JSR          LDMUL        ; FRO ← FRO*LOG10E

```

FRO ← 10^FRO (SEE COMMENTS FOR SEXPE)

RETURNS EXACT POWER OF 10 FOR INTEGERS.

```

A086          SEXPTE          ;10^X (SEE SHEP ATARI BASIC $DDCC EXP10)
A086 A9 00    LDA          #0           ;CLEAR TRANSFORM FLAG
A088 B5 F1    STA          DIGRT        ;XFMFLG
A08A A5 D4    LDA          FRO
A08C B5 F0    STA          FCHRFLG      ;SAME AS SGNFLG REMEMBER ARG SIGN
A08E 20 D2 A2 JSR          SABSVA       ;TAKE ABSOLUTE VALUE, A←FRO
A091 38       SEC
A092 E9 40    SBC          ##40
A094 30 27    BMI          SEXPO5      ;X<1 SO USE SERIES DIRECTLY (BUT CHECK FOR 0 FIRST)
A096 A2 E6    LDX          #FPSCR
A098 A0 05    LDY          #FPSCR/256
A09A 20 A7 DD JSR          FSTOR        ;SAVE IN SCRATCH REG
A09D 20 18 A3 JSR          SINTEG       ;GREATEST INTEGER ≤ X
A0A0 20 D2 D9 JSR          FPI         ;MAKE INTEGER
A0A3 B0 27    BCS          SFERR3      ;RETURN IF ERROR
A0A5 A5 D5    LDA          FRO+1       ;CHECK MSB
A0A7 D0 23    BNE          SFERR3      ;SHOULDN'T HAVE ANY -- RETURN IF ERROR
A0A9 A5 D4    LDA          FRO
A0AB B5 F1    STA          DIGRT        ;XFMFLG SAVE MULTIPLIER EXP
A0AD 20 AA D9 JSR          IFP         ;NOW TURN IT BACK TO FP
A0B0 20 B6 DD JSR          FMOVE       ;FR1 ← FRO
A0B3 A2 E6    LDX          #FPSCR      ;RELOAD FROM TEMP SCRATCH REG
A0B5 A0 05    LDY          #FPSCR/256
A0B7 20 89 DD JSR          FLDOR
A0BA 20 07 A3 JSR          SFSUB
A0BD          SEXPO5
A0BD A5 D4    LDA          FRO
A0BF D0 0B    BNE          SEXP10
A0C1 A9 01    LDA          #1          ;10^0 = 1
A0C3 20 53 A3 JSR          PSET0
A0C6 4C 12 DE JMP          EXP11       ;$DE12 DO 10^X, SKIPPING PLYEVL LDA XFMFLG
A0C9          SEXP10
A0C9 4C 03 DE JMP          EXP1        ;DO REST OF 10^X
A0CC          SFERR3
A0CC 38       SEC
A0CD 60       INIT      RTS

```


SILICON FLOATING POINT ROUTINE BY C. SHAW

FRO ← FRO - FR1 = SEXPTE (FR1 * SLOGTE (FRO))

USES MORE ACCURATE SEXPTE INSTEAD OF EXP10
 RETURNS EXACT INTEGER IF BOTH FRO AND FR1 ARE POSITIVE INTEGERS.
 RETURNS RECIPROCAL OF INTEGER IF BOTH ARE INTEGERS AND FR1 < 0
 RETURNS CARRY SET IF FRO < 0 OR (FRO = 0 AND FR1 < 0) OR OVERFLOW.
 0 < FR1 = 0 IF FR1 > 0
 0 < 0 = 1

ADCE	SPW20			
A00E A5 04	LDA	FRO	, FRO = 0?	
A000 D0 00	ENE	SPW20	, NO	
A002 A7 00	LDA	#0	, YES	
A004 A6 E0	LDX	FR1		
A006 30 78	EMI	PERR2	, FR1 < 0	0 ^ -X => ERROR
A008 D0 02	BNE	SPW10	, FR1 > 0	0 ^ X = 0
A00A A9 01	LDA	#1	, FR1 = 0	0 ^ 0 = 1
A00C				
A00C 4C 53 A3	JMP	PSET0		
A00F	SPW20			
A00F A5 E0	LDA	FR1		
A0E1 48	PHA		, SAVE FR1'S SIGN	
A0E2 29 7F	AND	#\$7F	, TAKE ABSOLUTE VALUE OF FR1	
A0E4 85 E0	STA	FR1		
A0E6 A2 82	LDX	#FTEMP	, SAVE FR1 IN FTEMP	
A0E8 A0 04	LDY	#FTEMP/256		
A0EA 20 D9 A2	JSR	FST1R		
A0ED 20 B6 DD	JSR	FMOVE		
A0F0 A9 01	LDA	#1		
A0F2 8D 81 04	STA	INTFLG	, ASSUME NOT BOTH INTEGERS	
A0F3 20 31 A5	JSR	STRUNC	, TRUNCATE FRO -- RETURN A=0 AND EQ IF FRO WAS ALREADY AN INTEGER	
A0F8 D0 0F	BNE	SPW50	, FRO WAS NOT AN INTEGER	
A0FA A2 82	LDX	#FTEMP	, LOAD SAVED VALUE INTO FRO	
A0FC A0 04	LDY	#FTEMP/256		
A0FE 20 89 DD	JSR	FLDOR		
A101 20 31 A3	JSR	STRUNC	, TEST FOR INTEGER	
A104 D0 03	BNE	SPW50	, NOT INTEGER	
A106 8D 81 04	STA	INTFLG	, 0 => BOTH INTEGER => RESULT SHOULD BE INTEGER	
A109	SPW50			
A109 A2 E0	LDX	#FR1		
A10B A0 00	LDY	#FR1/256	, FRO ← FR1 (MOVE ORIGINAL FRO BACK)	
A10D 20 89 DD	JSR	FLDOR		
A110 20 38 A1	JSR	SLOGTE	, LOG10(FRO)	
A113 80 3A	BCS	PERROR	, ERROR => POP FR1 SIGN AND RETURN	
A115 A2 82	LDX	#FTEMP	, LOAD FR1 AGAIN	
A117 A0 04	LDY	#FTEMP/256		
A119 20 98 DD	JSR	FLD1R		
A11C 20 DB DA	JSR	FMUL	, FRO ← FR1 * LOG10(BASE)	
A11F 80 2E	BCS	PERROR	, RETURN IF ERROR	
A121 20 86 AD	JSR	SEXPTE	, 10 ^ FRO	
A124 80 29	BCS	PERROR		
A126 AD 81 04	LDA	INTFLG	, SHOULD RESULT BE INTEGER?	
A129 D0 13	BNE	SPW80	, NO	
			, YES -- ROUND TO NEAREST INTEGER	
A12B A2 6C	LDX	#FHALF	, FR1 ← 0.5	
A12D A0 DF	LDY	#FHALF/256		
A12F 20 98 DD	JSR	FLD1R		
A132 A5 D4	LDA	FRO		
A134 1D 04	BPL	SROU10		

COLLEEN FLOATING POINT ROUTINES BY C SHAW

A134 A9 BF	LDA	#0F+\$00	, IF FRO < 0 THEN FR1 <- -0.5
A138 25 00	STA	FR1	
A13A	BRWVIO		
A13A 20 F7 A2	JSR	SFADD	, FRO <- FRO + FR1 (2-LEVEL RETURN IF ERROR)
A13D 20 31 A2	JSR	STRUNC	, TRUNCATE
A140	SPCHSQ		
A140 18	CLC		, INDICATE NO ERROR?
A141 68	PLA		, RELOAD FR1'S ORIGINAL SIGN
A142 10 00	BPL	PRTN	, DONE IF > 0
A144 20 B5 00	JSR	FMOVE	, IF < 0 THEN TAKE RECIPROCAL
A147 A9 01	LDA	#1	
A149 00 53 A3	JSR	PSET0	, FRO <- 1
A14C 4C 2B 00	JMP	FDIV	
A14F	PERROR		
A14F 58	PLA		, DISCARD FR1'S SIGN
A150	PERR2		
A150 38	SEC		, INDICATE ERROR
A151	PRTN		
A151 60	RTS		

COLLEEN FLOATING POINT ROUTINES BY C SHAW

FRO <- NATURAL LOG (FRO)

RETURNS CARRY SET IF FRO<=0

RETURNS EXACTLY 0 IF FRO = 1

A152 20 5E A1 SLN

A153 4C CD DE

JSR LOGCHK

JMP LOG

; CHECK FOR 0,1 (SPECIAL CASES)

FRO <- COMMON LOG (FRO) (LOG BASE 10)

SIMILAR TO SLN

A158 20 5E A1 SLOGTE

A158 4C D1 DE

JSR LOGCHK

JMP LOG10

A15E LOGCHK

A15E 38

A15F A5 D4

A161 F0 13

A163 30 11

A165 A2 05

A167

A167 B5 D4

A169 DD A9 A3

A16C D0 0A

A16E CA

A16F 10 F6

A171 68

A172 68

A173 4C 51 A3

A176

A176 68

A177 68

A178 60

LOGCHK

LOGCLP

PULRTN

RTURN2

SEC

LDA

BEQ

BMI

LDX

LDA

CMP

BNE

DEX

BPL

PLA

PLA

JMP

PCLRO

PLA

PLA

RTS

FRO

PULRTN

PULRTN

#FPREC-1

FRO, X

ONE, X

RTURN2

LOGCLP

PCLRO

; CHECK FOR 0,1

; LN(0), LOG(0) => ERROR

; <0 => ERROR => 2-LEVEL RETURN

; NOT 1 => OK

; SKIP LOGCHK RETURN

; LN(1)=LOGTEN(1)=0

COLLEEN FLOATING POINT ROUTINES BY C SHAW

BASIC SINE & COS ROUTINES

TO FIX BUGS OF VERSION 5.9 OF SHEP BASIC

BY DAVE & LARRY -- MODIFIED BY CAROL

4-6-79

MOD FUNCTION MAKES ROUTINES MORE ACCURATE FOR ANGLES > 360 DEGREES

COSINE ROUTINE -- ADD 90 OR PI/2 TO FRO TO DO SIN

```

A179          SCOS
A179 20 6F A3      JSR     SINMOD      ; TAKE ANGLE MOD 2*PI, 360
A17C 20 A0 A3      JSR     PIOVL      ; SET UP X & Y REGS TO LOAD PI/2 OR 90
A17F 20 98 DD      JSR     FLDIR      PUT PI/2 OR 90 INTO FR1
A182 20 F7 A2      JSR     SFADD      FRO=FRO + PI/2 (OR 90)

```

SINE ROUTINE

COMPUTE QUADRANT, GET FRACTION AND DO POLYNOMIAL,
THEN ADJUST FOR QUADRANT

```

A185          SSIN
A185 20 6F A3      JSR     SINMOD      ; TAKE ANGLE MOD 2*PI, 360
; FRO=FRO/(PI/2) OR FRO=FRO/90
A188 20 A0 A3      JSR     PIOVL      ; LOAD X & Y REGS TO GET PI/2 OR 90
A18B 20 0F A3      JSR     LDIDIV     FRO=FRO/FR1
; NOW HAVE 0-4 (NOT NECESSARILY INTEGER)

```

IF FRO NOW FRACTION, IT IS QUADRANT 0

ELSE, GET INTEGER OF FRO LSD

```

A18E A9 00          LDA     #0
A190 8D 80 04        STA     QUADFLG   ASSUME QUADRANT 0
A193 A5 D4          LDA     FRO       GET EXPONENT
A195 C9 40          CMP     #40       SUBTRACT 64 EXCESS
A197 90 19          BCC     SINF3     GO IF QUADRANT 0
A199 A5 D5          LDA     FRO+1     ; SHOULD BE 0, 1, 2, OR 3
A19B 8D 80 04        STA     QUADFLG   NOW HAVE QUADRANT (0,1,2, OR 3)
A19E 20 B6 DD        JSR     FMOVE     ; FR1 <- FRO
A1A1 20 31 A3        JSR     STRUNC    ; TRUNCATE FRO
A1A4 20 07 A3        JSR     SFSUB     ; FRO <- TRUNC(FRO)-FRO
A1A7 20 28 A3        JSR     SCHSG     ; CHANGE SIGN -- FRACTIONAL PART (FRO) = FRO - TRUNC (FRO)

```

IF ODD QUADRANT, SET FRO=1-FRO (90 DEGREE INVERT)

```

A1AA 4E 80 04        LSR     QUADFLG   IS IT ODD QUADRANT?
A1AD 90 03          BCC     SINF3     NO
A1AF 20 FD A2        JSR     ONESUB    ; FRO <- 1-FRO

```

SAVE ARG FOR LATER

```

A1B2          SINF3
A1B2 A2 E6          LDX     #FPSCR
A1B4 A0 05          LDY     #FPSCR/256
A1B6 20 A7 DD        JSR     FSTOR     ; FPSCR <- FRO

```

NOW COMPUTE SINE

THIS CODE TAKEN FROM BASIC 5.9 LINES 6760-6770

```

A1B9 20 EE A2        JSR     SSQUAR   FRO=X**2
A1BC A9 06          LDA     #NSCF
A1BE A2 AF          LDX     #SCDEF
A1C0 A0 A3          LDY     #SCDEF/256

```


A1DC A9 06	LDA	#NSCF	
A1BE A2 AF	LDX	#SCDEF	
A1C0 A0 A3	LDY	#SCDEF/256	

COLLEEN FLOATING POINT ROUTINES BY C SHAW

A1C2 20 40 DD	JSR	PLYEVL	EVALUATE P(X**2)
A1C5 A2 E6	LDX	#FPSCR	
A1C7 A0 05	LDY	#FPSCR/256	
A1C9 20 E8 A2	JSR	LDIMUL	FRO=SIN(X)=X*P(X**2)

			; IF LOWER QUADRANT (2 OR 3) THEN FRO=-(FRO)
A1CC 4E 80 04	LSR	QUADFLG	IS IT LOWER QUAD?
A1CF 90 03	BCC	SINF4	NO
A1D1 20 28 A3	JSR	SCHQSG	; YES

A1D4		SINF4	
------	--	-------	--

			; IF ABS(FRO) >= 1 THEN SET TO 1
A1D4 A5 D4	LDA	FRO	
A1D6 29 7F	AND	##7F	WITHOUT SIGN BIT
A1D8 C9 40	CMP	##40	COMPARE #40
A1DA 90 07	BCC	SINFIN	
A1DC A9 00	LDA	#0	
A1DE 85 D8	STA	FRO+4	; PERFORM PSEUDO INT(FRO) (CLEAR LAST 2 BYTES)
A1E0 85 D9	STA	FRO+5	
A1E2 18	SINFN2	CLC	; NO ERROR
A1E3 60	SINFIN	RTS	

FRO ← ARC TANGENT (FRO)

FROM SHEPARDSON ATARI BASIC 5.9 4-5-79 (MODIFIED)
 SAME ACCURACY AS SHEP VERSION -- USES FEWER BYTES

```

A1E4          SATAN
A1E4 A9 00    LDA    #0
A1E6 85 F0    STA    FCHRFLG      ; SIGN FLAG OFF
A1E8 85 F1    STA    DIGRT        ; AND TRANSFORM FLAG
A1EA A5 D4    LDA    FRO
A1EC AA      TAX
A1ED 29 7F    AND    #$7F
A1EF C9 40    CMP    #$40          ; CHECK X VS 1.0
A1F1 30 10    BMI    ATAN1        ; X<1 - USE SERIES DIRECTLY
A1F3 85 D4    STA    FRO          ; FORCE PLUS
A1F5 8A      TXA
A1F6 29 80    AND    #$80
A1F8 85 F0    STA    FCHRFLG      ; REMEMBER SIGN
A1FA E6 F1    INC    DIGRT
A1FC A2 EA    LDX    #FP9S
A1FE A0 DF    LDY    #FP9S/$100
A200 20 75 DE JSR    XFORM        ; CHANGE ARG TO (X-1)/(X+1)
A203          ATAN1
A203 A2 E6    LDX    #FPSCR        ARCTAN(X), -1<X<1 BY SERIES APPROX
A205 A0 05    LDY    #FPSCR/256    ; CAN'T USE FTEMP BECAUSE SATAN IS CALLED BY OTHER ROUTINES WHICH USE IT
A207 20 A7 DD JSR    FSTOR
A20A 20 EE A2 JSR    SSQUAR        ; X*X → FRO
A20D A9 0B    LDA    #NATCF
A20F A2 AE    LDX    #ATCDEF
A211 A0 DF    LDY    #ATCDEF/256
A213 20 40 DD JSR    PLYEVL        ; P(X*X)
A216 B0 26    BCS    ATNOUT        ; ERROR
A218 A2 E6    LDX    #FPSCR
A21A A0 05    LDY    #FPSCR/256
A21C 20 E8 A2 JSR    LD1MUL        ; X*P(X*X)
A21F A5 F1    LDA    DIGRT        ; WAS ARG XFORMED
A221 F0 10    BEQ    ATAN2        ; NO
A223 A2 F0    LDX    #PIQV4
A225 A0 DF    LDY    #PIQV4/256
A227 20 98 DD JSR    FLD1R
A22A 20 66 DA JSR    FADD
A22D A5 F0    LDA    FCHRFLG      ; GET ORG SIGN
A22F 05 D4    ORA    FRO
A231 85 D4    STA    FRO          ; ATAN(-X) = -ATAN(X)
A233          ATAN2
A233 A5 FB    LDA    RADFLG        ; RAD OR DEG
A235 F0 07    BEQ    ATNOUT        ; RAD - FINI
A237 A2 D9    LDX    #PIQV18
A239 A0 A3    LDY    #PIQV18/256
A23B 20 0F A3 JSR    LD1DIV        ; DIVIDE BY PI/180 TO CONVERT TO DEGREES
A23E          ATNOUT
A23E 60      RTS

```


COLLEEN FLOATING POINT ROUTINES BY C SHAW

FRO 2- SQUARE ROOT (FRO)

FROM SHEPARDSON ATARI BASIC 5.9 4-5-79 (MODIFIED)
 SAME ACCURACY AS SHEP VERSION -- USES FEWER BYTES

USES NEWTON-RAPHSON ITERATION

 $F(Y) = Y*Y - X$ $FPRIME(Y) = 2*Y$ $Y[I+1] = Y[I] - F(Y[I]) / FPRIME(Y[I]) = Y[I] + .5*((X/Y[I]) - Y[I])$

ERROR EXIT

A23F SQRERR
 A23F 38 SEC
 A240 60 RTS

ENTRY POINT

A241 SSQRT ; X<-SQRT(X)
 A241 A2 E0 LDX #FR1
 A243 20 46 DA JSR ZF1 ; FR1 <- ALL 0'S
 A246 A2 00 LDX #0
 A248 86 F1 STX DIGRT
 A24A E8 INX ; 1
 A24B 86 E1 STX FR1+1
 A24D A5 D4 LDA FRO
 A24F 30 EE BMI SQRERR ; ERROR IF <0
 A251 C9 3F CMP #3F
 A253 F0 09 BEQ FSQR ; X IN RANGE OF APPROX - GO DO IT TO IT
 A255 AA TAX
 A256 E8 INX
 A257 86 E0 STX FR1 ; MANTISSA = 1
 A259 86 F1 STX DIGRT ; NOT IN RANGE - TRANSFORM
 A25B 20 28 DB JSR FDIV ; X/100**N
 A25E FSQR ; SQR(X) 0.1<=X<1
 A25E A9 06 LDA #6
 A260 85 EF STA ESIGN
 A262 A2 E6 LDX #FSCR
 A264 A0 05 LDY #FSCR/256
 A266 20 A7 DD JSR FSTOR ; STASH X IN FSCR
 A269 A9 02 LDA #2
 A26B 20 FF A2 JSR INTSUB ; 2-X
 A26E A2 E6 LDX #FSCR
 A270 A0 05 LDY #FSCR/256
 A272 20 E8 A2 JSR LD1MUL ; X*(2-X) : 1ST APPROX
 A275 SQRLP
 A275 A2 EC LDX #FSCR1
 A277 A0 05 LDY #FSCR1/256
 A279 20 A7 DD JSR FSTOR ; Y->FSCR1
 A27C 20 B6 DD JSR FMOVE ; Y->FR1
 A27F A2 E6 LDX #FSCR
 A281 A0 05 LDY #FSCR/256
 A283 20 89 DD JSR FLDR
 A286 20 28 DB JSR FDIV ; X/Y
 A289 A2 EC LDX #FSCR1
 A28B A0 05 LDY #FSCR1/256
 A28D 20 98 DD JSR FLDR
 A290 20 60 DA JSR FSUB ; (X/Y)-Y
 A293 A2 6C LDX #FHALF

COLLEEN FLOATING POINT ROUTINES BY C SHAW

A295 A0 DF	LDY	#FHALF/256	
A297 20 E8 A2	JSR	LD1MUL	; .5*((X/Y)-Y)=DELTAY
A29A A5 D4	LDA	FRO	; DELTA 0
A29C F0 0E	BEG	SQRDON	
A29E A2 EC	LDX	#FSCR1	
A2A0 A0 05	LDY	#FSCR1/256	
A2A2 20 98 DD	JSR	FLD1R	
A2A5 20 66 DA	JSR	FADD	; Y=Y+DELTA Y
A2A8 C6 EF	DEC	ESIGN	; COUNT & LOOP
A2AA 10 C9	BPL	SQRLP	
A2AC			
A2AC A2 EC	SQRDON	LDX	#FSCR1
A2AE A0 05	LDY	#FSCR1/256	; DELTA = 0 - GET Y BACK
A2B0 20 89 DD	JSR	FLDOR	
A2B3 A2 E0	LDX	#FR1	WAS ARG TRANSFORMED?
A2B5 20 46 DA	JSR	ZF1	
A2B8 A5 F1	LDA	DIGRT	; FR1 <- ALL 0'S AGAIN
A2BA F0 16	BEG	SABSV4	
A2BC 38	SEC		; NO FINI
A2BD E9 40	SBC	##40	
A2BF 4A			
A2C0 08	LSR	A	; YES - TRANSFORM RESULT TO MATCH
A2C1 18	PHP		; DIVIDE EXP BY 2
A2C2 69 40	CLC		; SAVE CARRY (LSB OF DIGRT)
A2C4 85 E0	ADC	##40	
A2C6 A9 01	STA	FR1	
A2C8 28	LDA	#1	; MANTISSA = 1
A2C9 90 02	PLP		; RELOAD CARRY (LSBIT OF DIGRT)
A2CB A9 10	BCC	SQR2	; WAS EXP ODD OR EVEN
A2CD	LDA	##10	; ODD - MANT = 10
A2CD 85 E1	SQR2		
A2CF 20 DB DA	STA	FR1+1	
A2D2	JSR	FMUL	
A2D2 A5 D4	SABSV4		; SGR(X) = SGR(X/100**N) * (10**N)
A2D4 29 7F	LDA	FRO	; FRO <- ABSVAL(FRO) AC<-FRO
A2D6 85 D4	AND	##7F	
A2D8	STA	FRO	
A2D8 60	SABRTN		
	RTS		

COLLEEN FLOATING POINT ROUTINES BY C SHAW

THE FOLLOWING ROUTINES ARE CALLED BY THE PREVIOUS ROUTINES.
IN GENERAL, THEY DO A 2-LEVEL RETURN WITH CARRY SET IF AN
ERROR OCCURS, THUS BYPASSING THE REMAINDER OF THE CALLING ROUTINE

A2D9	FSTIR			; LIKE FSTOR EXCEPT USES FR1
A2D9 B4 FC	STX	FLPTR		
A2D9 B4 FD	STY	FLPTR+1		
A2DD A0 05	LDY	#5		
A2DF	FSLOR			
A2DF B9 E0 00	LDA	FR1,Y		
A2E2 91 FC	STA	(FLPTR),Y		
A2E4 B8	DEY			
A2E5 10 FB	BPL	FSLOR		
A2E7 60	RTS			
A2EB	L01MUL			; FRO <- FRO * DATA CONSTANT (ADDR IN X & Y)
A2EB 20 98 DD	JSR	FLD1R		
A2EB 4C F1 A2	JMP	SFMUL		
A2EE	ESQUAR			
A2EE 20 B6 DD	JSR	FMOVE		; FRO <- FRO * FRO
A2F1	SFMUL			; FRO <- FRO * FR1
A2F1 20 DB DA	JSR	FMUL		
A2F4 B0 16	BCS	CRYSND		
A2F6 60	RTS			
A2F7	SFADD			; FRO <- FRO + FR1
A2F7 20 66 DA	JSR	FADD		
A2FA B0 10	BCS	CRYSND		
A2FC 60	RTS			
A2FD A9 01	ONESUB	LDA	#1	; FRO <- 1-FRO
A2FF	INTSUB			; FRO <- A - FRO
A2FF 48	PHA			
A300 20 B6 DD	JSR	FMOVE		
A303 68	PLA			
A304 20 53 A3	JSR	PSET0		; A MUST BE FROM 0-9 OR BCD
A307	SFSUB			; FRO <- FRO - FR1
A307 20 60 DA	JSR	FSUB		
A30A	CRYCHK			; CHECK CARRY TO SEE IF THERE IS AN ERROR
A30A 90 02	BCC	RETURN		; RETURN IF CARRY CLEAR
A30C	CRYSND			; DO A 2-LEVEL RETURN IF ERROR
A30C 68	PLA			
A30D 68	PLA			
A30E 60	RETURN	RTS		
A30F	LD1DIV			; FRO <- FRO / (X,Y)
A30F 20 98 DD	JSR	FLD1R		
A312	SFDIV			; FRO <- FRO / FR1
A312 20 28 DD	JSR	FDIV		
A315 B0 F5	BCS	CRYSND		
A317 60	RTS			

COLLEEN FLOATING POINT ROUTINES BY C SHAW

A318		WINTER			; FRO <- INT(FRO)
A318	A5 D4		LDA	FRO	
A31A	48		PHA		
A31B	20 31 A3		JSR	STRUNC	; FRO <- TRUNC(FRO), RETURN EQ IF ALREADY INT
A31E	F0 2F		BEG	INTRT3	; INTEGER POP AND RETURN
A320	68		PLA		; RELOAD OLD FRO WITH SIGN
A321	10 0B		BPL	INTRT2	; POSITIVE

WAS NEGATIVE NON-INTEGERS

A323		SUBONE			; FRO <- FRO-1
A323	A9 01		LDA	#1	

A325		SUBINT			; FRO <- FRO - A
A325	20 FF A2		JSR	INTSUB	; FRO <- A-FRO
A328		SCHQSG			
A328	A5 D4		LDA	FRO	; FRO <- -FRO A<-FRO SET EQ/NE
A32A	F0 04		BEG	SCH10	
A32C	42 B0		EDR	##80	
A32E	85 D4		STA	FRO	
A330		SCH10			
A330	60		RTS		

GREATEST INT <= FRO

PART OF INT ROUTINE FROM SHEP ATARI BASIC B0D5-B0EE
DOES NOT AFFECT FR1?

A331	STRUNC			; TRUNCATE FRO RETURN A=0 AND EQ IF FRO WAS ALREADY AN INTEGER
A331 A5 D4		LDA	FRO	; GET EXPONENT
A333 29 7F		AND	##7F	; AND OUT SIGN BIT
A335 38		SEC		
A336 E9 3F		SBC	##3F	; GET LOCATION OF 1ST FRACTION BYTE
A338 10 02		BPL	XINT1	; IF >= 0 THEN BRANCH
A33A A9 00		LDA	#0	; ELSE SET =0
A33C	XINT1			
A33C AA		TAX		; PUT IN X AS INDEX INTO FROM
A33D A9 00		LDA	#0	; SET ACCUM TO ZERO FOR ORING
A33F A8		TAY		; ZERO Y
A340	INT2			
A340 E0 05		CPX	##PREC-1	; IS D.P. LOC >= -5?
A342 B0 07		BCS	INTRTN	; IF YES, LOOP DONE
A344 15 D5		ORA	FRO+1,X	; OR IN THE BYTE OF MANTISSA
A346 74 D5		STY	FRO+1,X	; ZERO BYTE
A348 E8		INX		; POINT TO NEXT BYTE
A349 D0 F5		BNE	INT2	; JUMP
A34B	INTRTN			
A34B 48		PHA		; SAVE OR OF ALL FRACTIONAL BYTES
A34C 20 00 DC		JSR	NORM	; NORMALIZE
A34E	INTRI3			
A34F 68		PLA		; RELOAD
A350 60	INTRI2	RTS		
A351	PCLRO			; CLEAR FRO
A351 A9 00		LDA	#0	RETURN WITH CARRY CLEAR (CC)
A353	PSET0			
A353 48		PHA		
A354 20 44 DA		JSR	ZFRO	; FRO <- 0
A357 68		PLA		
A358 F0 06		BEG	CLRTN	; 0 => ALL 0'S
A35A 85 D5		STA	FRO+1	
A35C A9 40		LDA	##40	; SET EXPONENT
A35E 85 D4		STA	FRO	
A360	CLRTN			
A360 1B		CLC		
A361 60		RTS		

SINE ROUTINES

```

A362          SINLD
A362 A2 DF      LDX      #PI2          ; LOAD 2*PI
A364 A0 A3      LDY      #PI2/256
A366 A3 FB      LDA      RADFLG
A368 E0 D8      BEQ      SNMOD3
A36A A2 E5      LDX      #C360
A36C A0 A3      LDY      #C360/256      ; DEGREES => LOAD 360
A36E          SNMOD3
A36E E0      RTS
A36F          SINMOD
A36F A3 D4      LDA      FRO          ; FIND ANGLE MOD 2*PI OR 360 DEPENDING ON RADFLG
A371 29 7F      AND      #$7F
A373 C9 A5      CMP      #$45
A375 D0 95      BCS      CRYEND      ; OUT OF RANGE -- 2-LEVEL RETURN
A377 A2 E6      LDX      #FPSCR
A379 A0 D5      LDY      #FPSCR/256      ; SAVE IN TEMP SCRATCH REG
A37B 20 A7 DD      JSR      FSTOR
A37E 20 62 A3      JSR      SINLD      ; LOAD 2*PI OR 360
A381 20 95 DD      JSR      FLD1R
A384 20 12 A3      JSR      SFDIV      ; ANGLE/360
A387 20 18 A3      JSR      SINTEG      ; INT(ANGLE/360)
A38A 20 62 A3      JSR      SINLD      ; LOAD 2*PI OR 360
A38D 20 95 DD      JSR      FLD1R
A390 20 F1 A2      JSR      SFMUL      ; INT(ANGLE/360)*360
A393 20 B6 DD      JSR      FMOVE
A396 A2 E6      LDX      #FPSCR      ; RELOAD ANGLE
A398 A0 D5      LDY      #FPSCR/256
A39A 20 B9 DD      JSR      FLD0R
A39D 4C 07 A3      JMP      SFSUB      ; ANGLE - INT(ANGLE/360)*360

```

```

A3A0          PLOVL
A3A0 A9 CD      LDA      ; LOAD X & Y REGS IN PREPARATION FOR LOADING REG 0 OR 1 WITH PI/2, 90 OR 100 IF GRAD
A3A2 18      CLC
A3A3 65 FB      ADC      #RADPI2
A3A5 AA      TAX
A3A6 A0 A3      LDY      #RADPI2/256
A3A8 60      RTS

```


COLLEEN FLOATING POINT ROUTINES BY C SHAW

DATA

A3A9 40 01 00	ONE	BYTE	\$40, \$01, 0, 0, 0, 0	1
A3AC 00 00 00				
A3AF	SCDEF			
A3AF BD 03 55		BYTE	\$BD, \$03, \$55, \$14, \$99, \$39	- 00000355149939
A3B2 14 99 39				
A3B5 3E 01 60		BYTE	\$3E, \$01, \$60, \$44, \$27, \$52	0 000160442752
A3B8 44 27 52				
A3BB BE 46 B1		BYTE	\$BE, \$46, \$B1, \$75, \$43, \$55	- 0046B1754355
A3BE 75 43 55				
A3C1 3F 07 96		BYTE	\$3F, \$07, \$96, \$92, \$62, \$39	0 0796926239
A3C4 92 62 39				
A3C7 BF 64 57		BYTE	\$BF, \$64, \$57, \$64, \$0B, \$67	- 6457640B67
A3CA 64 0B 67				
A3CD 40 01 57	RADPI2	BYTE	\$40, \$01, \$57, \$07, \$9B, \$32	(PI/2 = 1 57079B327 PART OF SCDEF
A3D0 07 9B 32				
A3D3 40 90 00		BYTE	\$40, \$90, 0, 0, 0, 0	180 (DEGREES)
A3D6 00 00 00				
A3D9 3F 01 7A	PI0V18	BYTE	\$3F, \$01, \$7A, \$53, \$29, \$25	(PI/180 = 017A532925 DEG-2RAD
A3DC 53 29 25				
A3DF 40 06 2E	PI2	BYTE	\$40, \$06, \$2E, \$31, \$85, \$31	(2*PI = 6 28318531
A3E2 31 85 31				
A3E5 41 03 60	COAD	BYTE	\$41, \$03, \$60, 0, 0, 0	1280
A3EB 00 00 00				

BEFA 00 A0	**BEFA			CARTRIDGE START INFO
BFFC 00 04	WORD	START		COLD/WARM START ADDRESS
BFFE CD A0	BYTE	0:4		RUN CARTRIDGE
	WORD	INTT		POWER UP START VECTOR
	END			

